

Optimization Show all work. Calculator permitted. Show all set-ups and analysis. Report all answers to 3 decimals and avoid intermediate rounding error.

Multiple Choice

1. An advertisement is run to stimulate the sale of cars. After t days, $1 \leq t \leq 48$, the number of cars sold is given by $N(t) = 4000 + 45t^2 - t^3$. On what day does the maximum rate of growth sales occur?

- (A) on day 17 (B) on day 13 (C) on day 15 (D) on day 16 (E) on day 14



2. A canvas wind shelter like the one above is to be built for use along parts of the American River. It is to have a back, two square sides, and a top. If $\frac{147}{2}$ square feet of canvas is to be used in the construction, find the depth of the shelter for which the space inside is maximized assuming all the canvas is used.

- (A) depth = 72 feet (B) depth = 7 4 feet (C) depth = 4 feet (D) depth = 7 feet (E) none of these

5. A point moves on the x -axis in such a way that its velocity at time t ($t > 0$) is given by $v(t) = \frac{\ln t}{t}$. At

what value of t does v attain its maximum?

- (A) 1 (B) e (C) e (D) $3e$ (E) There is no maximum value for v .

6. The derivative of $f(x) = \frac{x^4}{3} - \frac{x^5}{5}$ attains its maximum value at $x =$

- (A) -1 (B) 0 (C) 1 (D) $\frac{4}{3}$ (E) $\frac{5}{3}$

Multiple Choice

7. (Calculator Permitted) If the midpoints of 4 equal-width rectangles is used to approximate the area enclosed between the x-axis and the graph of $y = 4x - x^2$, the approximation is

- (A) 10 (B) 10.5 (C) 10.666 (D) 10.75 (E) 11

8. If $\int_2^5 f(x)dx = 18$, then $\int_2^5 (f(x) + 4)dx =$

- (A) 20 (B) 22 (C) 23 (D) 25 (E) 30

9. $\int_{-4}^4 (4 - |x|)dx =$

- (A) 0 (B) 4 (C) 8 (D) 16 (E) 32

10. If $\int_a^b f(x)dx = a + 2b$, then $\int_a^b (f(x) + 3)dx =$

- (A) $a+2b+3$ (B) $3b-3a$ (C) $4a-b$ (D) $5b-2a$ (E) $5b-3a$

11. The expression $\frac{1}{20} \left(\sqrt{\frac{1}{20}} + \sqrt{\frac{2}{20}} + \sqrt{\frac{3}{20}} + K + \sqrt{\frac{20}{20}} \right)$ is a Riemann sum approximation for

- A) $\int_0^1 \sqrt{\frac{x}{20}} dx$ B) $\int_0^1 \sqrt{x} dx$ C) $\frac{1}{20} \int_0^1 \sqrt{\frac{x}{20}} dx$ D) $\frac{1}{20} \int_0^1 \sqrt{x} dx$ E) $\frac{1}{20} \int_0^{20} \sqrt{x} dx$

12. If $f(x)$ is represented by the table below, approximate $\int_1^{9.6} f(x)dx$

Use as many subintervals as the data allows:

x	1	2.5	4	6	8	8.8	9.6
$f(x)$	4	3	2	3	5	6	4

a) left end point Riemann sum

b) right end pt Riemann sum

c) midpoint

d) trapezoid